

Capacity formulas

Capacity

Machine requirements for single products

$$M = \frac{Dp}{N[1-(C/100)]}$$

Machine requirements for multiple products

$$M = \frac{[Dp + (D/Q)s]_{product\ 1} + [Dp + (D/Q)s]_{product\ 2} + \dots + [Dp + (D/Q)s]_{product\ n}}{N[1 - (C/100)]}$$

M = Number of machines

D = Yearly demand

p = processing time per product

Q = Batch size

s = setup time per batch

N = Total operating time per year

C = Desired capacity cushion (expressed in %)

Break-even analysis

Total cost $C = F + c \times Q$

Total revenue $R = p \times Q$

Break even quantity $Q = \frac{F}{(p-c)}$

C = Total cost

F = Fixed cost

c = variable cost

Q = Quantity of sold products/services

R = Total revenue

p = revenue per sold unit

Forecasting formulas, KPP227

Linear regression:

$$Y = a + bX$$

$$b = \frac{\Sigma XY - n\bar{X}\bar{Y}}{\Sigma x^2 - n\bar{X}^2}$$

$$a = \bar{Y} - b\bar{X}$$

Forecast accuracy (Linear regression):

Correlation coefficient:
$$r = \frac{n \Sigma XY - \Sigma X \Sigma Y}{\sqrt{[n \Sigma X^2 - (\Sigma X)^2][n \Sigma Y^2 - (\Sigma Y)^2]}}$$

Coefficient of determination:
$$r^2 = \frac{a \Sigma Y + b \Sigma XY - n\bar{Y}^2}{\Sigma Y^2 - n\bar{Y}^2}$$

Standard error of the estimate:
$$\sigma_{YX} = \sqrt{\frac{\Sigma Y^2 - a \Sigma Y - b \Sigma XY}{n-2}}$$

Weighted moving average

$$F_{t+1} = W_1 D_t + W_2 D_{t-1} + \dots + W_n D_{t-n+1}$$

Exponential smoothing

$$F_{t+1} = \alpha D_t + (1 - \alpha) F_t$$

$$F_{t+1} = F_t + \alpha (D_t - F_t)$$

Exponential smoothing with trend

$$A_t = \alpha D_t + (1 - \alpha)(A_{t-1} + T_{t-1})$$

$$T_t = \beta (A_t - A_{t-1}) + (1 - \beta) T_{t-1}$$

$$F_{t+1} = A_t + T_t$$

A_t = exponential smoothed average of the series in period t

T_t = exponential smoothed average of the trend in period t

α = smoothing parameter for average (value 0-1)

β = smoothing parameter for trend (value 0-1)

T_{t+1} = Forecast for period t+1

Forecast errors

Forecast error

$$E_t = D_t - F_t$$

Average forecast error

$$\bar{E} = \frac{CFE}{n}$$

Mean square error

$$MSE = \frac{\sum E_t^2}{n}$$

Mean absolute deviation

$$MAD = \frac{\sum |E_t|}{n}$$

Standard deviation

$$\sigma = \sqrt{\frac{\sum (E_t - \bar{E})^2}{n-1}}$$

Mean absolute percentage error

$$MAPE = \frac{\sum [|E_t|(100)]/D_t}{n}$$

Tracking signal

$$Tracking\ Signal = \frac{CFE}{MAD}$$

Inventory management

Holding cost

$$\text{Holding cost} = \frac{Q}{2}(H)$$

Ordering-/setup cost

$$\text{Ordering or setup cost} = \frac{D}{Q}(S)$$

Material handling cost

$$C = \frac{Q}{2}(H) + \frac{D}{Q}(S)$$

Economic order quantity

$$EOQ = \sqrt{\frac{2DS}{H}}$$

Time between orders

$$TBO_{EOQ} = \frac{EOQ}{D}$$

Q = Order quantity

H = Holding cost per item

D = Forecasted demand

S = Setup cost per order

Continuous review (Q) system

Inventory position

$$IP = OH + SR - BO$$

IP = Inventory Point

OH = On-hand inventory

SR = Scheduled receipts

BO = Back orders

Re-order point

$$R = \bar{d}L + \text{Safety stock}$$

\bar{d} = Average demand per time unit

L = constant lead time In time units

Standard deviation of demand during lead time:

$$\sigma_{dLT} = \sqrt{\sigma_d^2 L} = \sigma_d \sqrt{L}$$

Safety stock: = $Z\sigma_{dLT}$

Periodic review (P) system

$$T = \bar{d}(P + L) + z\sigma_{(P+L)} = \bar{d}(P + L) + z\sigma_d \sqrt{P + L}$$

T = average demand during the protection interval + safety stock for protection interval

P = length of time between reviews

Noninstantaneous replenishment

$$\text{Maximum cycle inventory: } I_{max} = \frac{Q}{p}(p - d) = Q \left(\frac{p-d}{p} \right)$$

p = production rate

d = demand rate

Q = lot size

$$\text{Total annual cost: } C = \frac{I_{max}}{2}(H) + \frac{D}{Q}(S)$$

$$\text{Total annual cost: } C = \frac{Q}{2} \left(\frac{p-d}{p} \right) (H) + \frac{D}{Q}(S)$$

$$\text{Economic production lot size: } ELS = \sqrt{\frac{2DS}{H}} \sqrt{\frac{p}{p-d}}$$

I = Inventory

D = annual demand

p = production rate

d = demand rate

Q = lot size

H = holding cost

S = ordering/setup cost

Quantity discounts

Total annual material cost: $C = \frac{Q}{2}(H) + \frac{D}{Q}(S) + PD$

Q = lot size

H = holding cost

D = annual demand

S = ordering/setup cost

P = Price/unit

D = Demand rate

One period decisions

Payoff: $\text{If } Q \leq S \Rightarrow \text{Payoff} = pQ$

$$\text{If } Q > S \Rightarrow \text{Payoff} = pD - ld$$

p = profit/unit

Q = Purchased quantity

D = actual demand

l = loss/unit

d = number of disposed items

Location formulas, KPP227

Location

Load distance

$$ld = \sum_i l_i d_i$$

Euclidian distance

$$d_{AB} = \sqrt{(X_A - X_B)^2 + (Y_A - Y_B)^2}$$

Rectilinear distance

$$d_{AB} = |X_A - X_B| + |Y_A - Y_B|$$

Center of gravity

$$X^* = \frac{\sum l_i X_i}{\sum l_i}$$

$$Y^* = \frac{\sum l_i Y_i}{\sum l_i}$$

Waiting lines formulas, KPP227

Waiting lines

Interarrival times

$$P_n = \frac{(\lambda T)^n}{n!} e^{-\lambda T} \text{ for } n = 1, 2, \dots$$

P_n = Probability of n arrivals in T time periods

λ = Average numbers of customer arrivals per period

Service time distribution

$$P_{(t \leq T)} = 1 - e^{-\mu T}$$

μ = Average number of customers completing service per period

t = service time of the customer

T = target service time

Single server model

Average utilization of the system

$$\rho = \frac{\lambda}{\mu}$$

Average number of customers in the system

$$L = \frac{\lambda}{\mu - \lambda}$$

Average number of customers in the waiting line

$$L_q = \rho L = \frac{\lambda^2}{\mu(\mu - \lambda)}$$

Average time spent in the system including service

$$W = \frac{1}{\mu - \lambda}$$

Average waiting time in line

$$W_q = \rho W = \frac{\lambda}{\mu(\mu - \lambda)}$$

Probability that n customers are in the system

$$P_n = (1 - \rho)\rho^n$$

Probability that 0 customers are in the system

$$P_0 = 1 - \frac{\lambda}{\mu}$$

Probability that less than k customers are in the system

$$P_{n < k} = 1 - \left(\frac{\lambda}{\mu}\right)^k$$

Probability of more than k customers are in the system

$$P_{n > k} = \left(\frac{\lambda}{\mu}\right)^{k+1}$$

